

# Design of Intersections for Safety and Efficiency

Chapter objectives covered in CE361: By the end of this chapter the student will be able to:

1. Find the critical gap for an unsignalized intersection approach (given data of accepted and rejected gaps)
2. Analyze the sight distances at an intersection for possible installation of stop or yield signs
3. Determine when an intersection warrants the installation of a traffic signal
4. Design signal settings for intersections so that drivers will not face a dilemma zone
5. Estimate the stopped delay for an approach to an intersection

# 8.1 Analysis of Non-signalized Intersections

By the end of this section, the student will be able to...

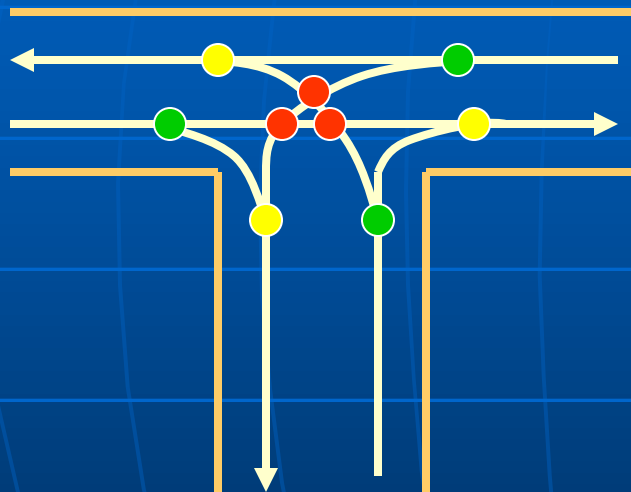
- Objectives of 8.1
  - Determine gaps in traffic that are acceptable to motorists
  - Determine whether to install a yield sign or stop sign, based on critical approach speed

# 8.1 Analysis of Non-signalized Intersections

- Right of way needs to be assigned to reduce potential conflicts and crashes.
- See the next slide to see how many potential conflict points exists in a T and a 4-leg unsignalized intersection.

# Conflict points at unsignalized intersections

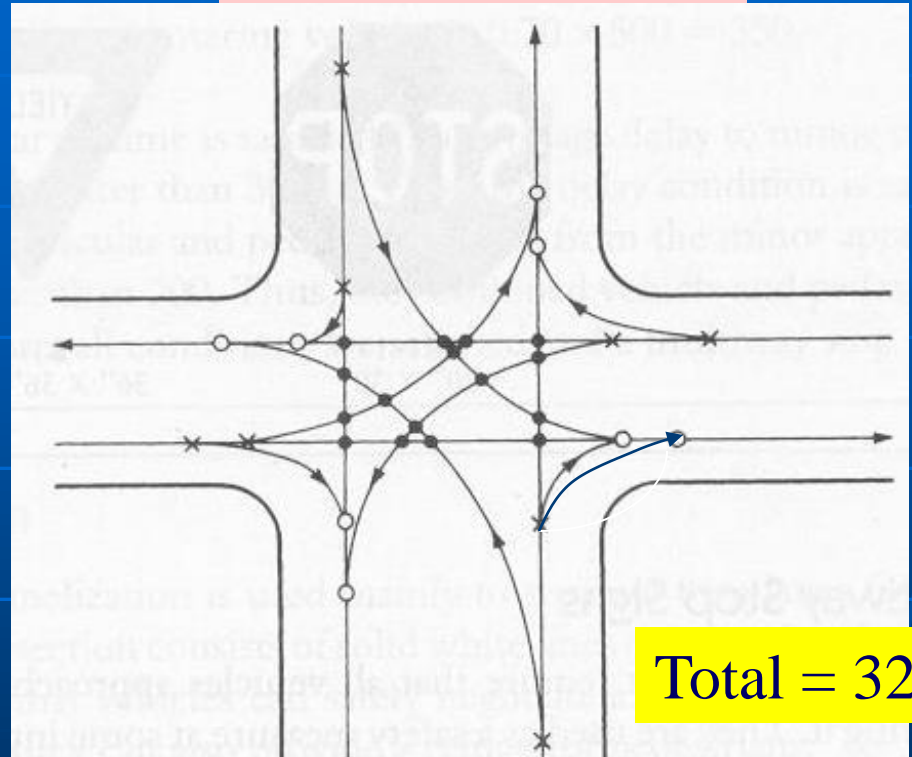
## T intersection



- Crossing = 3
- Merging = 3
- Diverging = 3

**Total = 9**

## 4-leg intersection

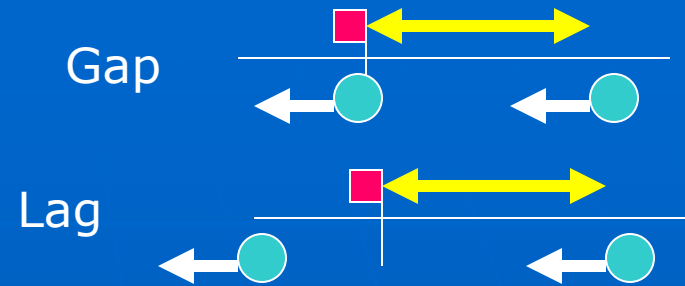


**Total = 32**

- Merging conflict points = 8
- × Diverging conflict points = 8
- Crossing conflict points = 16

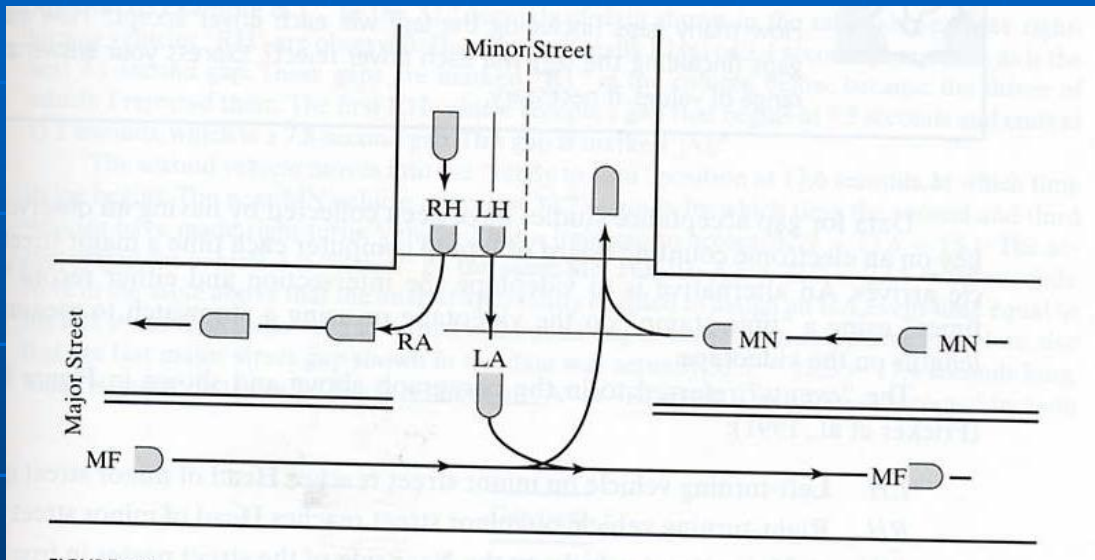
## 8.1.1 Gap acceptance

First, terminology...



- **Headway** – time elapsed between the front bumper of one vehicle and the front bumper of the following vehicle passing a given point
- **Gap** – time elapsed between the rear bumper of one vehicle and the front bumper of the following vehicle passing a given point
- **Lag** – time elapsed between the arrival of a minor-street vehicle ready to move into the major street and the arrival of the front bumper of the next vehicle in the major traffic stream
- **Accepted gap or lag** – gap or lag that the driver of a minor street vehicle uses to move into the major street
- **Rejected gap or lag** – gap or lag that the driver of a minor street vehicle waiting to enter the major street does not accept
- **Untested gap** – no minor street vehicle was present
- **Critical gap** – the minimum size gap that a particular driver will accept

# Events in gap acceptance analysis



**LH** = LT veh at Head of minor st. queue

**RH** = RT veh at Head of minor st. queue

**MN** = Major st. vehicle on the Near side

**MF** = Major st. vehicle on the Far side

**LA** = LH vehicle Accepts the gap

**RA** = RH vehicle Accepts the gap

# Example 8.1

Key for understanding this table → Check the arrival of MN after the arrival of RH.

Time (sec)	Event	Remarks	Time (sec)	Event	Remarks
0	RH	RT veh at head	17.6	RH	RT veh at head
3.4	RH MN	Rejected lag 3.4 sec	17.6	RA	Accepted lag 15.1 sec (32.7-17.6)
7.5	MN	Rejected gap 4.1 sec (7.5-3.4)	23.4	RH	RT veh at head
11.4	RA	Accepted gap 7.8 sec (15.3-7.5)	23.4	RA	Accepted lag 9.3 sec (32.7-23.4)
15.3	MN	MN arrives. Gap 7.8 sec	32.7	MN	MN arrives. Gap 17.4 sec (32.7-15.3)



# Mr. Raff's method simplified

Mr. Raff



The gap for which the number of accepted gaps shorter than it is equal to the number of rejected gaps longer than it.

$$t_c = t_1 + \frac{(t_2 - t_1)[R(t_1) - A(t_1)]}{[A(t_2) - R(t_2)] + [R(t_1) - A(t_1)]}$$

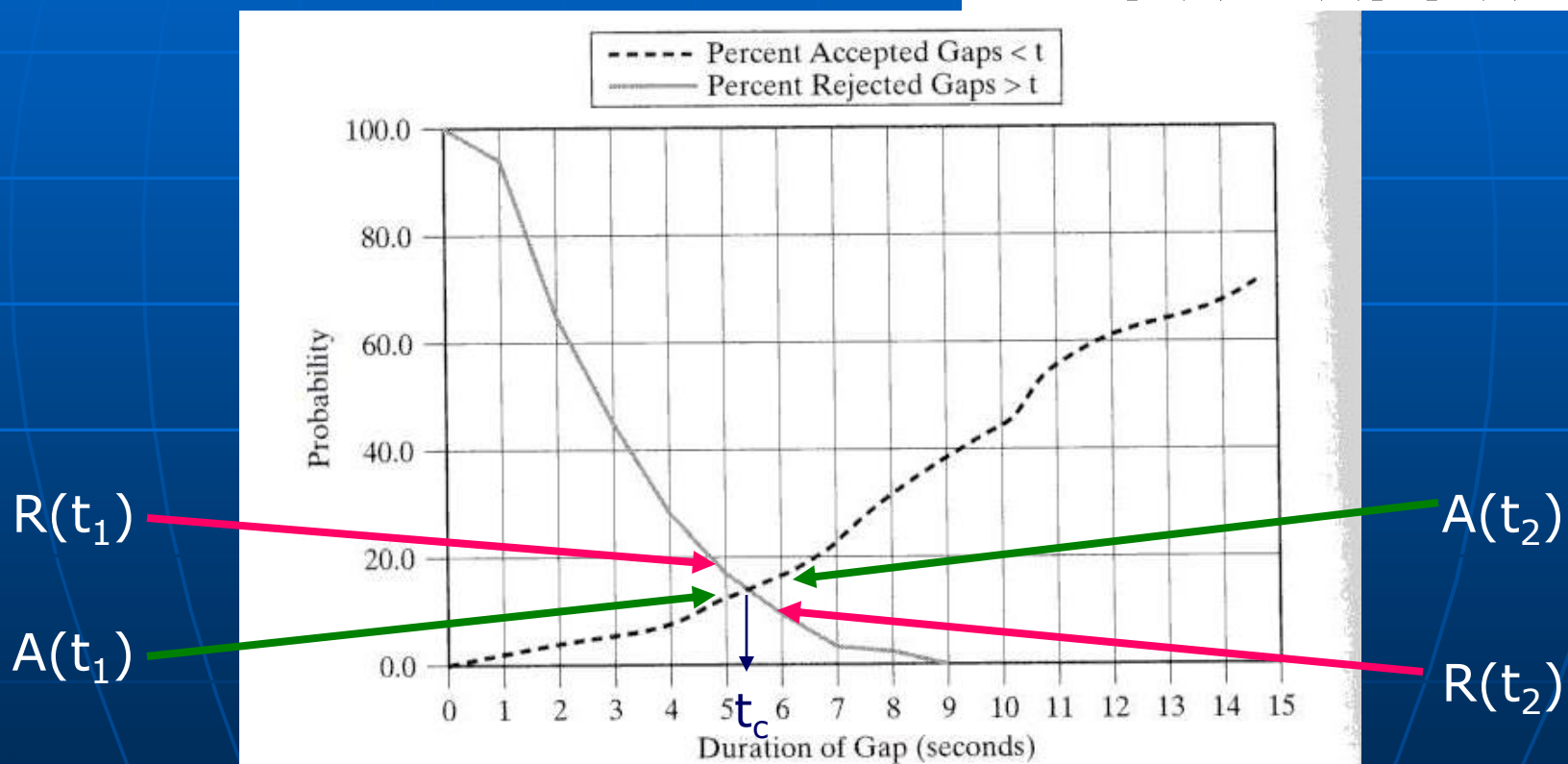


FIGURE 8.3

Cumulative distribution curves for accepted and rejected gaps.

See Table 8.1 for data.



## 8.1.2 Stop, Yield, or No Control at Urban Intersections

# Hierarchy of intersection control

Intersection Control Options: How much judgment can drivers safely exercise to avoid collisions? Three levels of control are available.

Level I	Passive control – basic rules of the road apply <ul style="list-style-type: none"><li>➤ No control</li><li>➤ Guide signs only</li><li>➤ Warning signs with or without guide signs</li></ul>
Level II	Assignment of ROW to major street or rotational ROW <ul style="list-style-type: none"><li>➤ YIELD control (roundabouts are in this category)</li><li>➤ Two-way STOP control</li><li>➤ All-way STOP control</li></ul>
Level III	Positive alternate assignment of exclusive ROW <ul style="list-style-type: none"><li>➤ Traffic signals: 2-phase, multiphase</li><li>➤ Traffic control agent/officer</li></ul>



# Warrants for YIELD sign

The YIELD sign may be warranted:

- A. When the ability to see all potentially conflicting traffic is sufficient to allow a road user traveling at the posted speed, 85<sup>th</sup> percentile speed, or the statutory speed to pass through the intersection or stop in a safe manner.
- B. If controlling a merge-type movement on the entering roadway where acceleration geometry or sight distance is not adequate for merging traffic operations.
- C. At a second crossroad of a divided highway, where the median width is 30ft or greater. A STOP sign may be installed at the entrance to the first roadway of a divided highway, and a YIELD sign may be installed at the entrance to the second roadway.
- D. At an intersection where a special problem exists and where engineering judgment indicates that the problem is susceptible to correction by use of a YIELD sign.



## Warrants for two-way STOP sign

Because the STOP sign causes a substantial inconvenience to motorists, it should be used only where warranted. A STOP sign may be warranted where one or more of the following conditions exist:

- A. Intersection of a less important road with a main road where application of the normal ROW rule would not be expected to provide reasonably safe operation.
- B. Street entering a through highway or street.
- C. Unsignalized intersection in a signalized area.
- D. High speeds, restricted view, or crash records indicate a need for control by the STOP sign.

## ■ The critical approach speed (CAS)

- If the computed speed is between 10 and 15 mph, a YIELD sign is appropriate.
- If the computed speed is less than 10 mph, a STOP sign must be installed
- At computed speeds higher than 15 mph, the CAS does not by itself justify a STOP or YIELD sign. Further analyses may be needed. (MUTCD has a set of warrants for Yield and Stop sign. Approach speed is not the only concern)

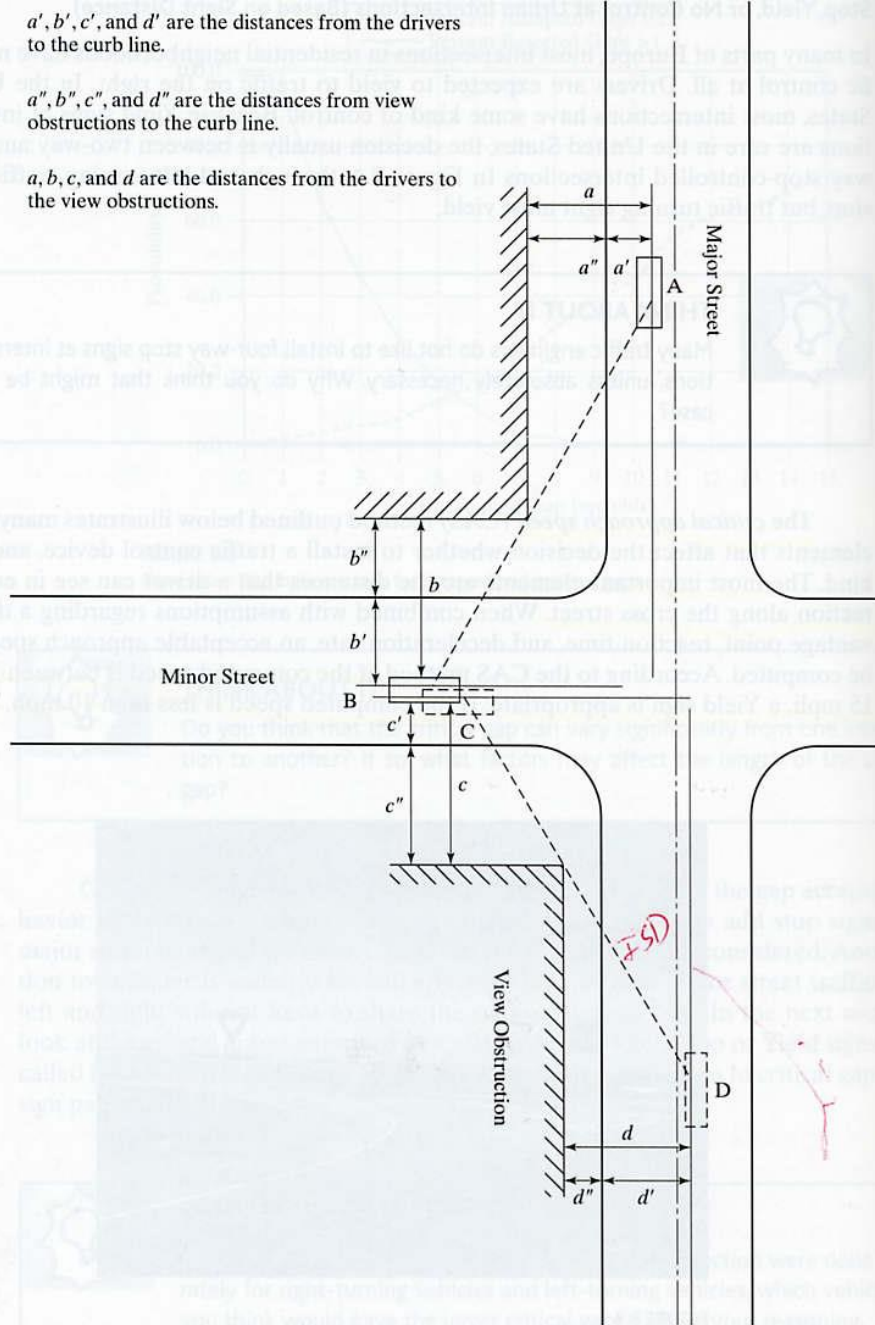
After checking the need for a yield or stop sign, check the intersection sight distance (ISD) for vehicles on the major street. If ISD is inadequate, stop signs on the major street may be called for. (see page 426 for  $t_c$  values.  $t_c = 7.5$  sec for passenger cars,  $t_c = 9.5$  for single unit trucks, and  $U, t_c = 11.5$  sec for combination trucks)

$$ISD = 1.47 * V * t_c$$

$a'$ ,  $b'$ ,  $c'$ , and  $d'$  are the distances from the drivers to the curb line.

$a''$ ,  $b''$ ,  $c''$ , and  $d''$  are the distances from view obstructions to the curb line.

$a$ ,  $b$ ,  $c$ , and  $d$  are the distances from the drivers to the view obstructions.



# The CAS Method

$a''$ ,  $b''$ ,  $c''$ , and  $d''$  are measured at the site.

$a'$ ,  $b'$ ,  $c'$ , and  $d'$  are computed as follows:

- $a' = 12$  ft with parking,  $a' = 6'$  without parking.
- $b' = \min\{\frac{1}{2}W + 3 \text{ ft}; W - 12 \text{ ft}\}$
- $c' = 12$  ft with parking,  $c' = 6'$  without parking.
- $d' = \frac{1}{2}W + 3$  ft

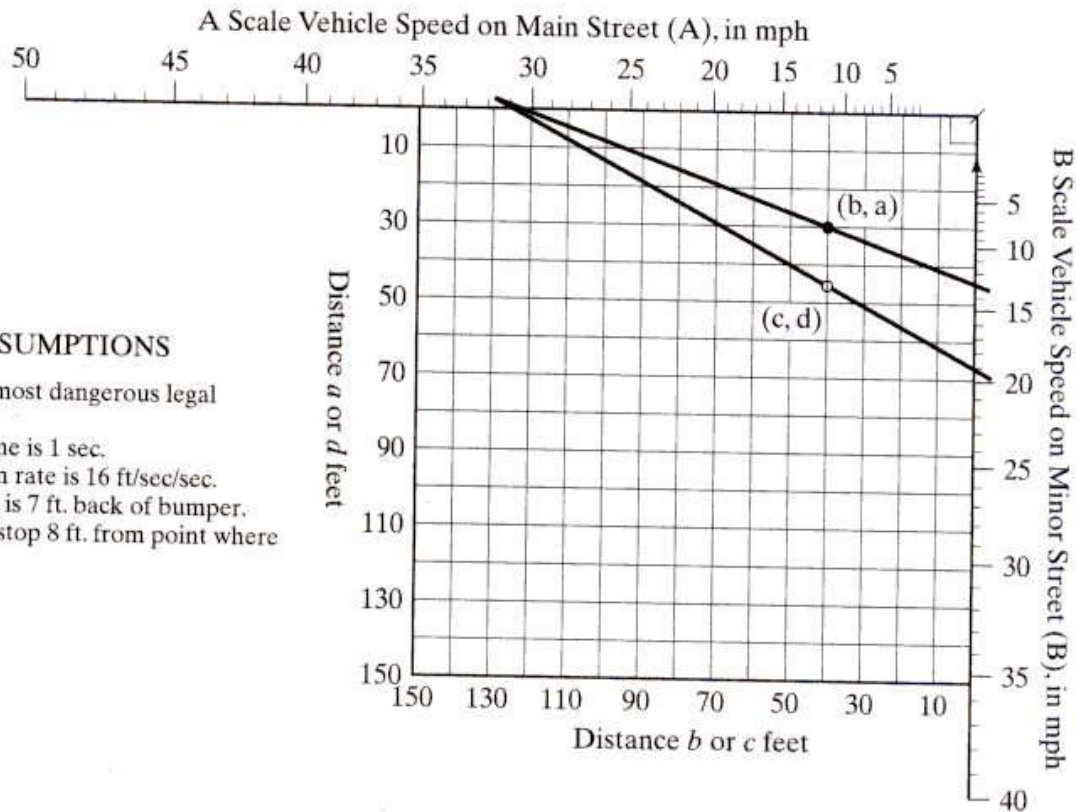
3 ft = distance between the centerline and the driver's head.

$\frac{1}{2}W$  = distance between the center line and the curb

$W$  = street width

FIGURE 8.5  
Typical critical approach speed problem. Source: Federal Highway Administration, 1983, p. 2-18.

# The CAS Method (cont.)



## ASSUMPTIONS

1. Vehicles in most dangerous legal position.
2. Reaction time is 1 sec.
3. Deceleration rate is 16 ft/sec/sec.
4. Driver's eye is 7 ft. back of bumper.
5. Vehicle can stop 8 ft. from point where paths cross.

**FIGURE 8.6**

Critical approach speed chart. Source: Federal Highway Administration, 1983, p. 2-17.

Find:

$$a = a' + a''$$

$$b = b' + b''$$

$$c = c' + c''$$

$$d = d' + d''$$

- Place points (b,a) and (c,d) in Fig 8.6.
- Extend lines starting from the 85<sup>th</sup>-percentile speed on Main St., passing through the two points.
- Read Minor street speed from B scale.
- Use the lower speed to make a decision:  $\leq 10$  mph – stop sign;  $10 < \text{speed} \leq 15$  mph – yield sign. Otherwise, needs a study

We will walk through Example 8.2.



# 8.2 Signal Warrants & Stopping Distance at Signalized Intersections

By the end of this section, the student will be able to...

- Objectives of 8.2
  - Determine when to install a traffic signal.
  - Determine whether a dilemma zone exists on the approach to a signalized intersection



# 8.2 Signal Warrants & Stopping Distance at Signalized Intersections

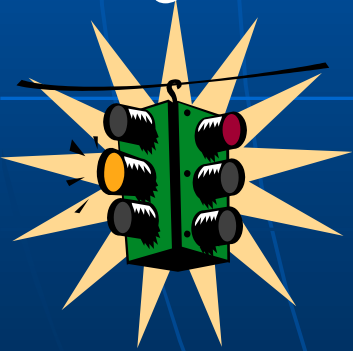
**(a) When should traffic signals be installed?**

**(b) When do signal timings create a hazardous situation for drivers**

## 8.2.1 Warrant Analysis

**MUTCD 2000 has 8 warrants for a traffic signal. They are guides, not specifications. Use professional judgments.**

### Signals



Covered  
in detail  
in CE562.

- ❖ **Warrant 1: Eight-hour vehicular volume**
- ❖ **Warrant 2: Four-hour vehicular volume**
- ❖ **Warrant 3: Peak hour**
- ❖ **Warrant 4: Pedestrian volume**
- ❖ **Warrant 5: School crossing**
- ❖ **Warrant 6: Coordinated signal system**
- ❖ **Warrant 7: Crash experience**
- ❖ **Warrant 8: Roadway network**

# Signal warrant 1A: 8-hour volume

**Min. vehicle volume:** Principal factor is the intersection traffic volume. Must satisfy for each of any 8 hour of an average day.

## Volume Requirements for Minimum Vehicular Volumes Warrant

Number of Lanes for Moving Traffic on Each Approach		Vehicles per Hour on Major Street (total of both approaches)	Vehicles per Hour on Higher-Volume Minor-Street Approach (one direction only)
Major Street	Minor Street		
1	1	500	150
2 or more	1	600	150
2 or more	2 or more	600	200
1	2 or more	500	200

➤ May reduce the values by 30% if the 85<sup>th</sup> percentile speed on the major approach is greater than 40 mph or population is less than 10,000 (built-up area of isolated community).

# Signal warrant 1B

**Interruption of continuous traffic:** The volume requirements must be met for each of any 8 hours of an average day.

## Minimum Vehicular Volumes for Interruption of Continuous Traffic Warrant

Number of Lanes for Moving Traffic on Each Approach		Vehicles per Hour on Major Street (total of both approaches)	Vehicles per Hour on Higher-Volume Minor-Street Approach (one direction only)
Major Street	Minor Street		
1	1	750	75
2 or more	1	900	75
2 or more	2 or more	900	100
1	2 or more	750	100

➤ May reduce the values by 30% if the 85<sup>th</sup> percentile speed on the major approach is greater than 40 mph or population is less than 10,000 (built-up area of isolated community).

# Signal warrant 1C

**Combination of warrants:** Only in exceptional cases. When none of them are satisfied but when the first two warrants of Warrant 1 are satisfied to the extent of 80% of the stipulated volumes.

## Example 8.3

- By overhead transparency

## 8.2.2 Reacting to a Changing Traffic Signal – a story of “dilemma zone”

**“... the term “amber” has been changed to “yellow,” and the yellow interval simply means “the red interval is coming.” The preferred reaction is to try to stop. However, it is possible that there is not sufficient distance for the car to stop, and the car would be in the intersection when the cross traffic gets the green light. The driver could be accused of “running the red light.”**

**Note that currently “running the red light” means the vehicle enters the intersection after the red light was turned on. Once the vehicle is in the intersection, you are not “running the red light” when the cross traffic gets the green light. Most of the signal has an all-red interval after the yellow interval, which was meant to clear the intersection for conflicting movements.**

# Safely stop at or before the stop bar or clear the intersection & dilemma zone

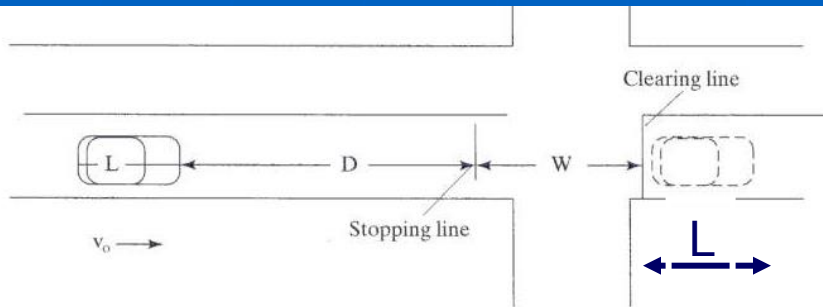
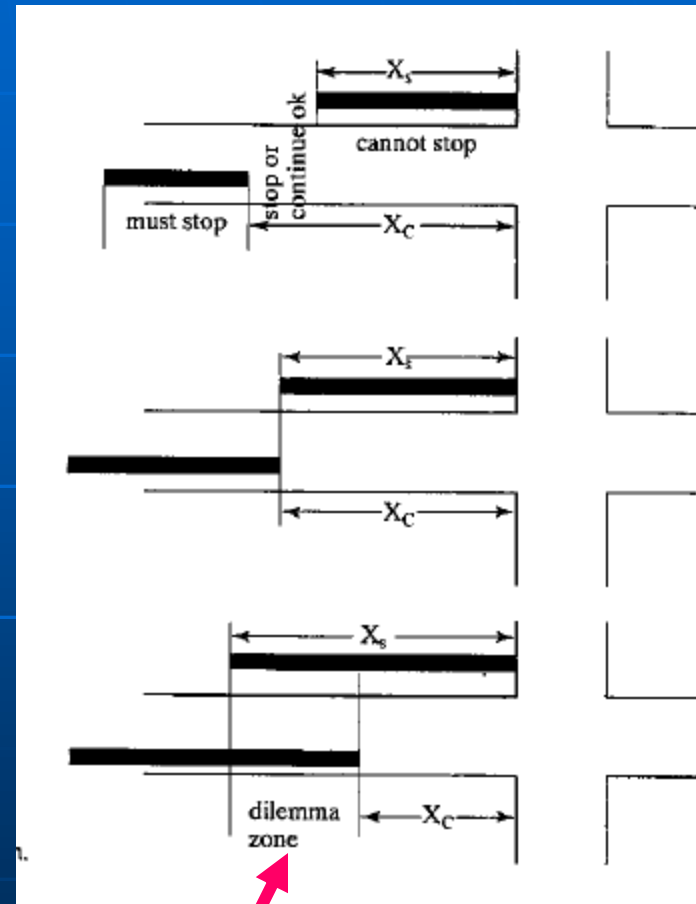


FIGURE 8.9  
Vehicle approaching a signalized intersection.

where  $d_{\text{brake}}$  = the deceleration rate for braking to a stop

$$t_s = \text{time to stop} = \frac{v_0}{d_{\text{brake}}}$$

$a_{\text{acc}}$  = the acceleration rate to increase speed when going through the intersection



Dilemma zone: Cannot stop or cannot finish crossing ( $X_s > X_c$ )

To safely stop:

$$X_S = D \geq v_0 t_r + \frac{v_0^2}{2d_{\text{brake}}}$$

To safely clear:

$$X_C = D \leq v_0 t_Y - (W + L)$$

Usually it is assumed the car will not accelerate (conservative estimate). Add this formula to eq. 8.3.



# Walk through Example 8.4 & 8.5

# Safely stop at or before the stop bar or clear the intersection & dilemma zone (using SSD formula)

Cannot clear but can safely stop

Cannot safely stop but can clear

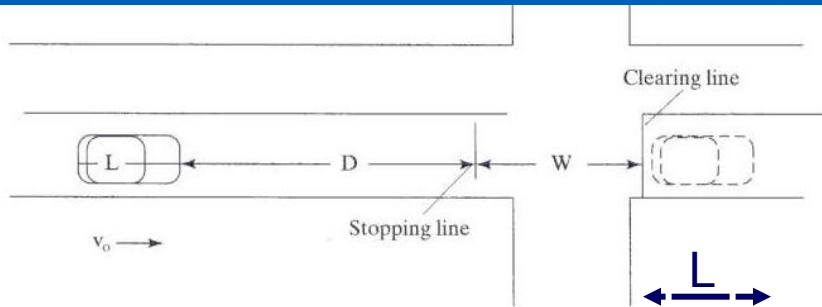


FIGURE 8.9  
Vehicle approaching a signalized intersection.

where  $d_{\text{brake}}$  = the deceleration rate for braking to a stop

$$t_s = \text{time to stop} = \frac{v_o}{d_{\text{brake}}}$$

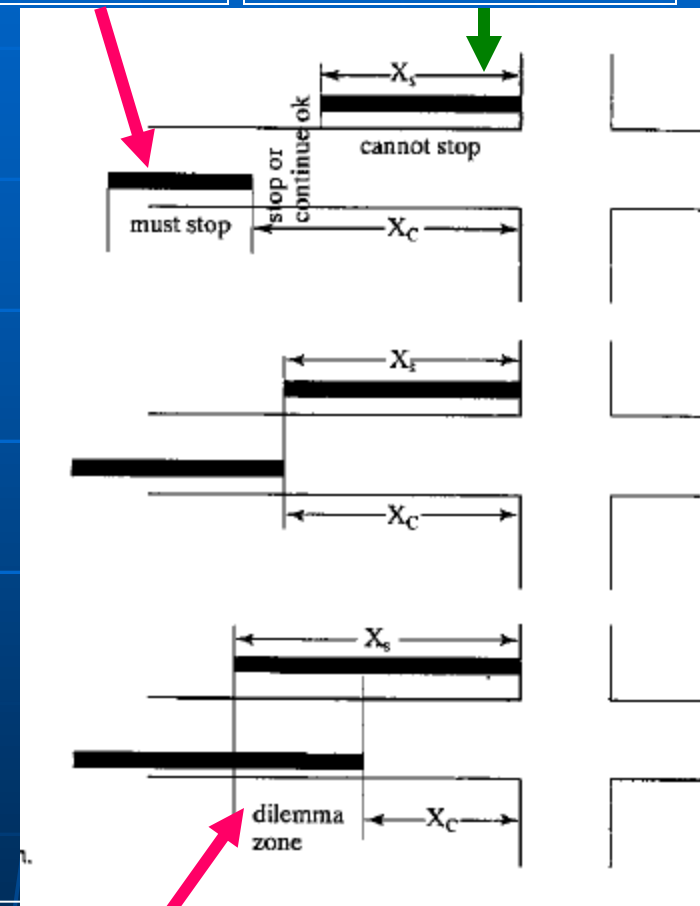
$a_{\text{acc}}$  = the acceleration rate to increase speed when going through the intersection

To safely stop:

$$X_S = D \geq v_o t_r + \frac{v_o^2}{2g(f \pm G)}$$

To safely clear:

$$X_C = D \leq v_o t_Y - (W + L)$$



Dilemma zone: Cannot stop or cannot finish crossing ( $X_S > X_C$ )

# Eliminating the dilemma zone

When  $X_c = X_o$ , there is no dilemma zone - at least theoretically.

$$v_o t_Y - (W + L) = v_o t_r + \frac{v_o^2}{2g(f \pm G)}$$

$$v_o t_Y = v_o t_r + \frac{v_o^2}{2g(f \pm G)} + (W + L)$$

$$t_Y = t_r + \frac{v_o}{2g(f \pm G)} + \frac{(W + L)}{v_o}$$

# Solution to Example 8.4 using SSD formula

The minimum distance needed to stop  $X_c$  is:

$$\begin{aligned} X_s &= v_o t_r + v_o^2 / [2 * g (f \pm G)] \\ &= 30 * 1.47 * 1.5 + (30 * 1.47)^2 / [2 * 32.2 * 0.35] \\ &= 66.15 + 86.28 = 152.4 \text{ ft } (G = 0, \text{ flat profile}) \end{aligned}$$

The maximum distance from which the vehicle can safely clear the intersections is:

$$\begin{aligned} X_c &= v_o t_y - (W + L) = 30 * 1.47 * 4 - (60 + 16) \\ &= 176.4 - 76 = 100.4 \text{ ft} \end{aligned}$$

$X_s > X_c$  (152.4 ft > 100.4 ft), hence a dilemma zone exists.

Its length is 152.4 ft – 100.4 ft = 52 ft. The driver's claim cannot be dismissed, but now the issue becomes whether the vehicle was in the dilemma zone when the light changed to yellow.

# Solution to Example 8.5 using SSD formula

$$\begin{aligned} \text{A)} \quad t_Y &= t_r + \frac{v_o}{2g(f \pm G)} + \frac{(W + L)}{v_o} \\ &= 1.5 + \frac{30 * 1.47}{2 * 32.2 * 0.35} + \frac{(60 + 16)}{30 * 1.47} \\ &= 5.18 \end{aligned}$$

Since  $t_Y$  remains to be 4 seconds, AR = 1.18 seconds

$$\begin{aligned} \text{B)} \quad v_o t_Y &= v_o t_r + \frac{v_o^2}{2g(f \pm G)} + (W + L) \\ v_o * (4 + 2) &= v_o * 1.5 + \frac{v_o^2}{2 * 32.2 * 0.35} + (60 + 16) \\ v_o * 4.5 &= \frac{v_o^2}{22.54} + 76 \\ 0.0444 * v_o^2 - 4.5 * v_o + 76 &= 0 \end{aligned}$$

Solving for  $V_o$ ,  $V_o =$   
79.93 ft/s or 21.40 ft/sec

or

$V_o = 54.4$  mph or 14.6  
mph

# 8.3 Analysis of Signalized Intersection

By the end of this section, the student will be able to...

## ■ Objectives of 8.3

- Summarize a signal timing plan for a given intersection in a concise format.
- Use time-space diagram to analyze systems of traffic signal settings
- (Actuated signals, 8.3.3, and delay estimation, 8.3.4. are not covered in CE361. They are discussed in detail in CE562 Traffic Engineering)

# 8.3 Analysis of Signalized Intersection

## 8.3.1 Traffic signal timing

Cycle length

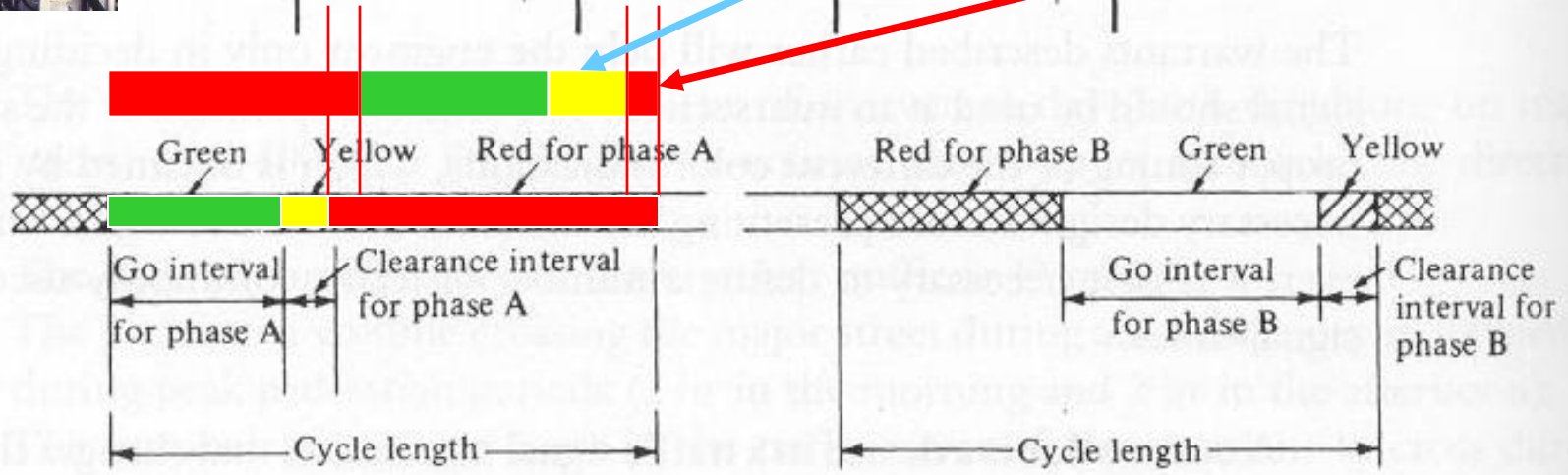
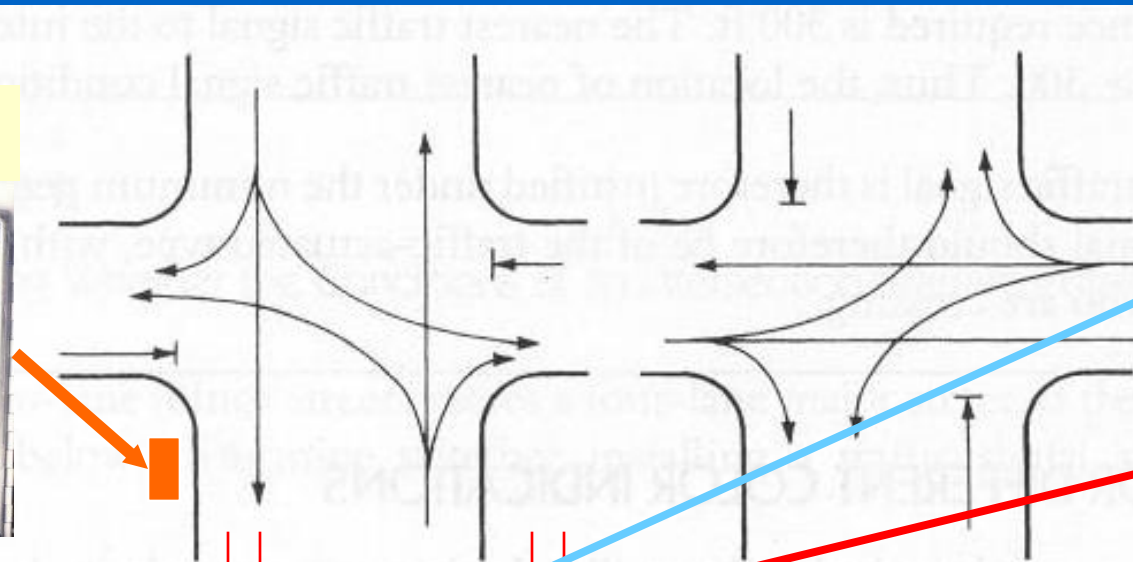
Phase

Interval

Change interval

All-read interval  
(clearance interval)

Controller



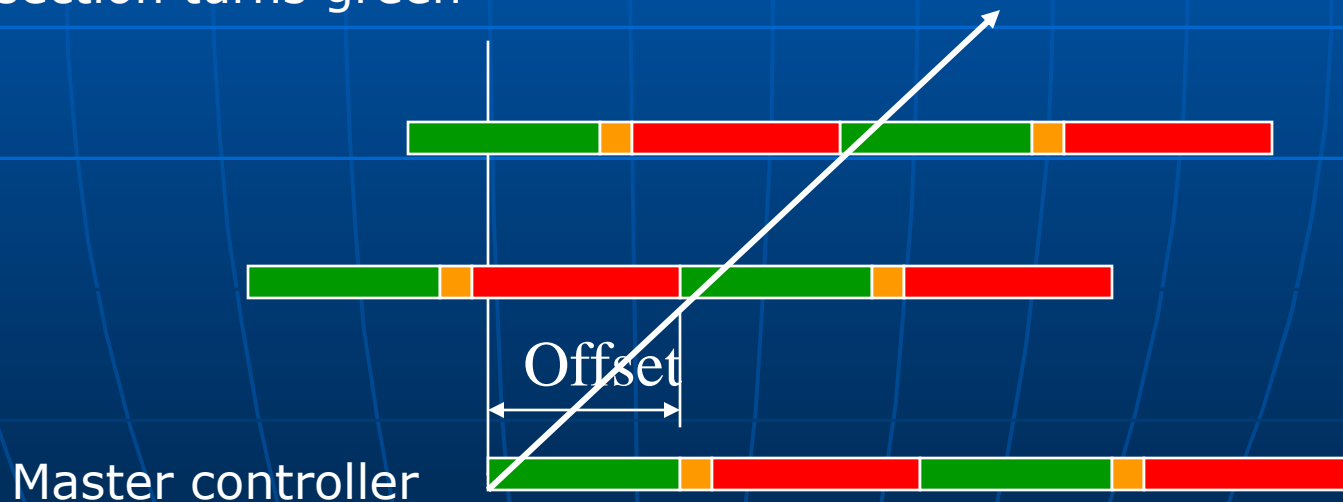
(a) Phase A

(b) Phase B



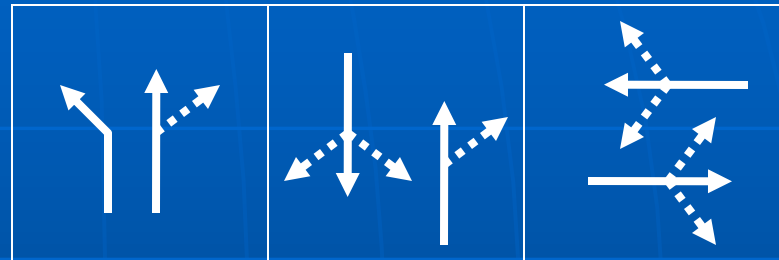
# Terms related to signal timing (cont)

- **Phase** = A signal phase consists of a green interval (G), plus the change (Y) and clearance intervals (AR) that follow it. It is a set of intervals that allows a designated movement or set of movements to follow and to be safely halted before release of a conflicting set of movements.
- **Offset** = The difference between the time when the upstream intersection turns green and the downstream intersection turns green



Time(sec)	Interval	Interval length	Signal Indication	Coliseum Ave.				
				NBLT	NB TH/RT	SB Vehs	EB Vehs	WB Vehs
1				G = 14	G = 38	R = 19	R = 44	R = 44
2								
3								
4								
5								
6								
7								
8								
9								
10								
11								
12								
13								
14	1	14	Green					
15				Y = 4				
16								
17								
18	2	4	Yellow					
19	3	1	All Red?	R = 57				
20						G = 19		
21								
22								
23								
24								
25								
26								
27								
28								
29								
30								
31								
32								
33								
34								
35								
36								
37								
38	4	19	Green					
39				Y = 4	Y = 4			
40								
41								
42	5	4	Yellow					
43				R = 33	R = 33			
44	6	2	All Red					
45						G = 26	G = 26	
46								
47								
48								
49								
50								
51								
52								
53								
54								
55								
56								
57								
58								
59								
60								
61								
62								
63								
64								
65								
66								
67								
68								
69								
70	7	26	Green					
71						Y = 4	Y = 4	
72								
73								
74	8	4	Yellow					
75	9	1	All Red				R = 1	R = 1
Total		75 seconds						

Table 8.4 shows a traffic signal-timing form

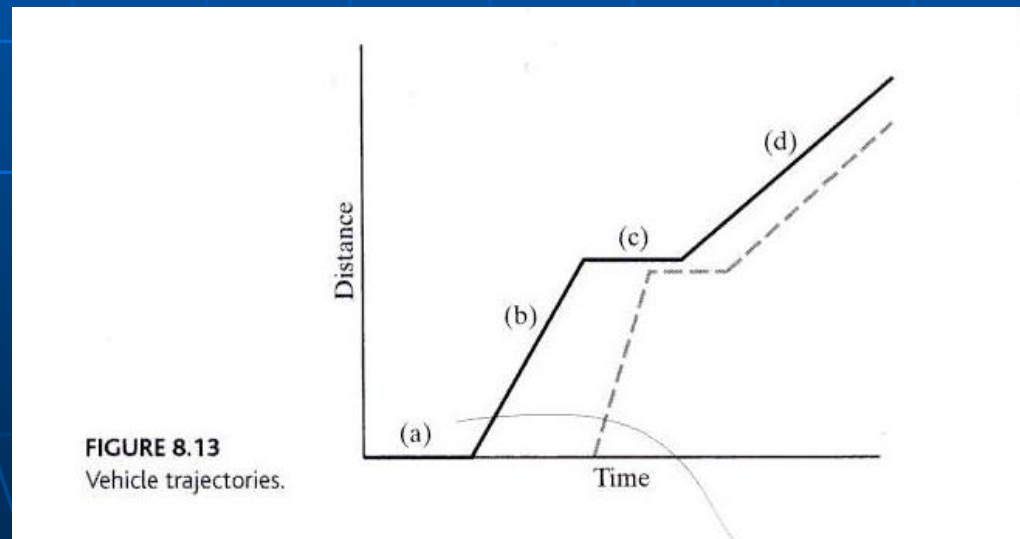


You can calculate interval lengths from the given G-Y-R data, but a diagram like this gives you a clearer picture of what's happening in the cycle. Look at these diagrams as you read the explanation of the timing form in the text (Last paragraph of p.436 and Example 8.6).

## 8.3.2 Time-Space Diagrams

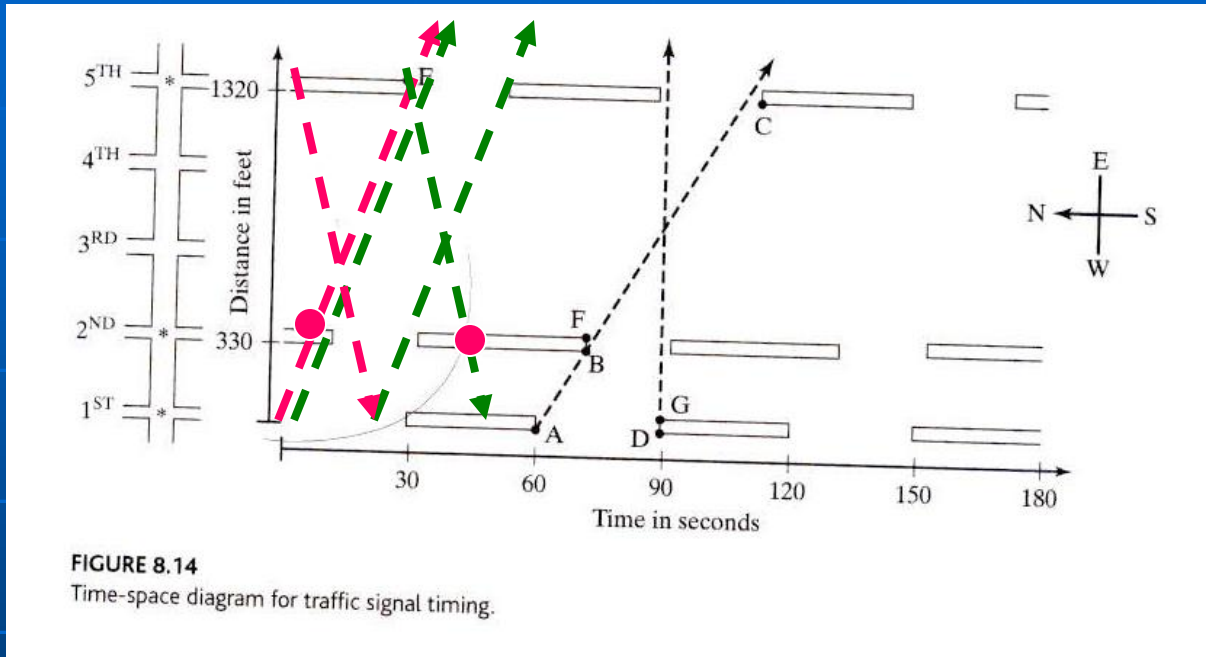
T-S diagram: A scaled chart that shows trajectories of vehicles traveling downstream or upstream

- (a) Stopped (distance/time = 0/time = 0 speed)
- (b) Traveling downstream at a speed
- (c) Stopped again
- (d) Traveling downstream again

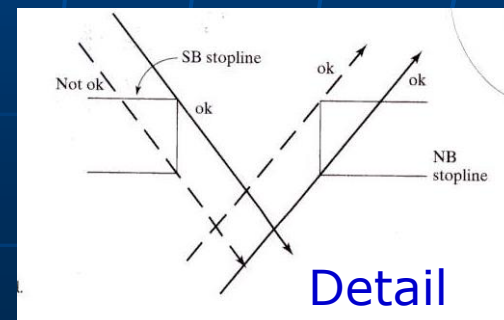


# Time-space diagram for signal coordination

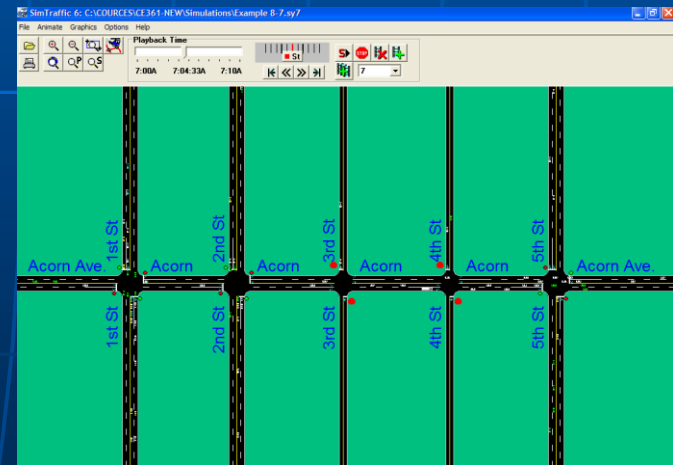
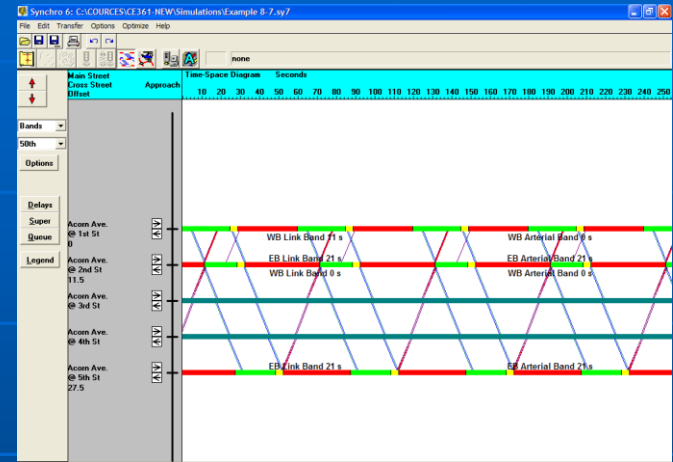
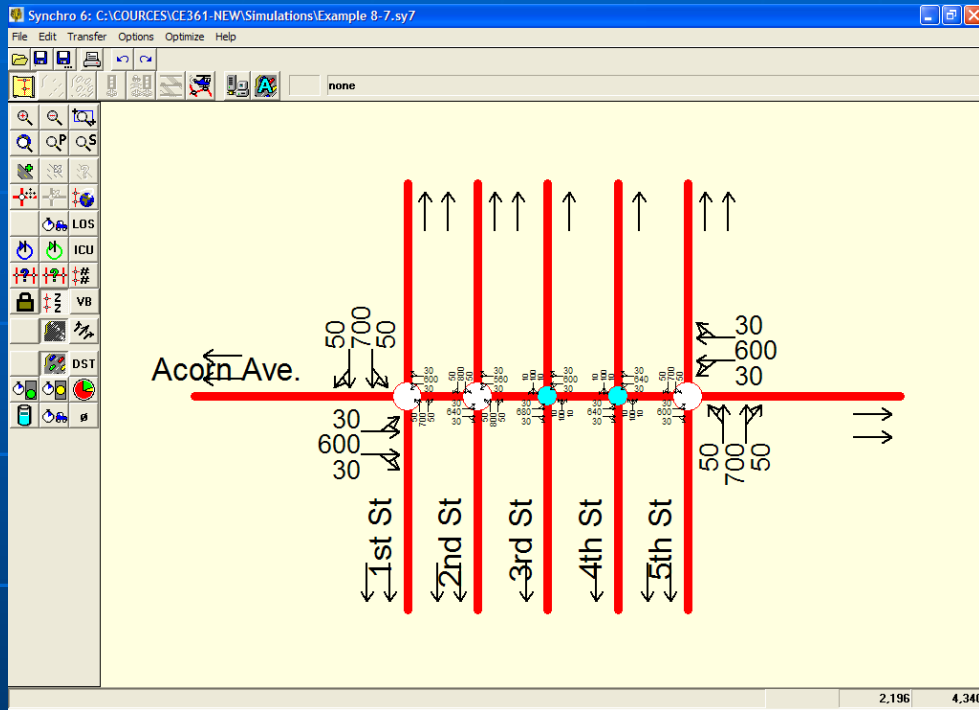
(Fig 8.14 is for Example 8.7)



Once the timing design of each signal is completed, offsets of the signals can be adjusted to achieve the speed and green band desired. But depending on the block length and timing, you may not be able to get exactly what you want.



# Example 8.7 by Synchro 7 software



We will extensively discuss signal timing issues in CE562.